

Heat transfer between a horizontal flat surface and the natural environment

I.F. Lombaard¹ and D.G. Kröger²

(First received June 2000; Final version April 2001)

The objective of this study was to obtain a correlation for the effective convective heat transfer between a horizontal 1 m × 1 m surface and the environment. Tests were conducted on a suitable surface at a particular location exposed to different solar radiation intensities, ambient temperatures and wind velocities. Based on the experimental data, a correlation for the effective heat transfer coefficient, that takes into consideration natural convection, forced convection (wind) and solar radiation (clear sky), is presented. This coefficient can be employed to predict the heat transfer on the surface of solar collectors having geometries similar to the present test set-up and operating under similar environmental conditions.

Nomenclature

a	Constant, W/m ² K
b	Constant
c	Constant
c_p	Specific heat capacity, J/kg K
Gr	Grashof number, $2(T_p - T_a)gL^3\rho^2/((T_p + T_a)\mu^2)$
h	Convective heat transfer coefficient, W/m ² K
h_w	Heat transfer coefficient due to wind, W/m ² K
I_h	Solar radiation on horizontal surface, W/m ²
n	Number of data points
k	Thermal conductivity of air, W/mK
L	Length of plate side, m
Nu	Nusselt number, hL/k
Pr	Prandtl number, $\mu c_p/k$
p_a	Atmospheric pressure, N/m ²
q_c	Convection heat transfer rate, W/m ²
q_r	Radiation heat transfer rate, W/m ²
Re	Reynolds number, $\rho v_w/\mu$
T_a	Ambient air temperature, K
T_p	Mean plate temperature, K
T_{sky}	Sky temperature, K
v_w	Wind speed, m/s

Greek letters

α_p	Absorption coefficient of plate
ρ	Density of air, kg/m ³
ε_p	Emissivity of plate
μ	Dynamic viscosity of air, kg/m s
σ	Stefan-Boltzman constant, 5.67×10^{-8} W/m ² K ⁴

Subscripts

a	Atmospheric
cor	Correlation
ex	Experiment
l	Laminar flow
nc	Natural convection
t	Turbulent flow
w	Wind

Introduction

In the evaluation of the performance of solar collectors, suitable equations are required to quantify the heat transfer between the collector cover and the environment. Although extensive research and development have been done to date, uncertainty still exists concerning reliable equations to predict these transfer rates.

Duffie,¹ referring to convective heat transfer due to wind over the surface of a solar collector, stated that "from the preceding discussion it is apparent that the calculation of wind induced heat transfer coefficients is not well established". More recently Sharples and Charlesworth⁵ came to the conclusion that "... as experiments come closer to resembling 'real' collector situations so more discrepancies and inconsistencies are found both between measured results from different experiments and with standard flat-plate forced convection relationships for h_w ".

Discrepancies are due to various reasons, including the fact that the definition of the convective heat transfer coefficient is not always consistent. Often the geometry of the apparatus and its environment is not adequately described. Unless wind tunnel tests for evaluating the convective heat transfer coefficient are conducted under conditions of turbulence levels, similar to those found under windy ambient conditions, resultant heat transfer correlations cannot be expected to be in agreement.

In general, the convective heat transfer coefficient due to wind on the surface of a collector cover is expressed by a relation of the form

$$h_w = a + bv_w^c \quad (1)$$

¹Student, Department of Mechanical Engineering, University of Stellenbosch

²Professor, Department of Mechanical Engineering, University of Stellenbosch, Private Bag X1, Matieland, 7602 South Africa

where a , b and c are constants.

It is obvious from the many studies that have been reported to date, that this very simple equation cannot be expected to model what is really a very complex heat transfer process.

According to eqn. (1), $h_w = a$ when $v_w = 0$. Values of 'a' quoted in the literature vary from 2.8 according to Watmuff *et al.*⁷ to 10.03 according to Kumar *et al.*² The fact that h_w has a finite value in the absence of wind, can only mean that under these conditions heat transfer occurs due to natural convection, and h_w is unlikely to have a constant value.

As eqn. (1) is not written in dimensionless form, it does not make provision for changes in the thermophysical properties of the air when operating under different ambient conditions.

In the following analysis and experiment the above concerns are addressed in more detail. An effective heat transfer coefficient for a specific plate geometry operating in a particular environment is clearly defined and quantified by means of a correlation based on measured data.

Analysis

Consider the upper surface of a polystyrene horizontal flat plate that is exposed to the environment as shown in Figure 1. By applying an energy balance to a unit area of the upward facing surface find

$$I_h = (1 - \alpha_p) I_h + q_r + q_c \quad (2)$$

where I_h is the solar radiation (clear sky in present investigation) on a unit horizontal surface area, α_p is the plate absorption coefficient, while q_r and q_c are the long-wave radiation and convection heat transfer rates in W/m^2 . Conduction losses through the polystyrene plate are assumed to be negligible.

The heat flux due to radiation from the upper surface of the plate to the sky can be expressed as

$$q_r = \sigma \epsilon_p (T_p^4 - T_{\text{sky}}^4) \quad (3)$$

where ϵ_p is the emissivity of the plate, T_p is the mean plate surface temperature, and according to Swinbank⁶ the sky temperature in Kelvin is

$$T_{\text{sky}} = 0.0552 T_a^{1.5}$$

where T_a is the ambient air Kelvin temperature.

Although other expressions for sky temperature are available, this particular expression is chosen in order to define a corresponding convective heat transfer coefficient.

The convective heat flux can be expressed as

$$q_c = h (T_p - T_a) \quad (4)$$

with h defining the effective convective heat transfer coefficient which will be determined experimentally in this study.

Thus from eqn. (2), together with eqn. (3) and eqn. (4), it follows that

$$h = \frac{\alpha_p I_h - \sigma \epsilon_p \{T_p^4 - (0.0552 T_a^{1.5})^4\}}{T_p - T_a} \quad (5)$$

This relation defines the convective heat transfer coefficient. The latter can be determined experimentally if I_h , α_p , ϵ_p , T_p and T_a are measured.

Experiment

Experiments were conducted in order to determine the convective heat transfer coefficient between a $1 \text{ m} \times 1 \text{ m}$ horizontal polystyrene plate (50-mm polystyrene) on a solid $1 \text{ m} \times 1 \text{ m}$ square pedestal having a height of 1.05 m and highly reflective sides. Five fine type T thermocouples, having short response times, were located on the upper surface in positions as shown in Figure 2.

The test facility was located 100 m above sea level at 33.98°S latitude and 18.85°E longitude. During the tests solar radiation I_h (on a horizontal surface) ranged between 250 and 1030 W/m^2 , while wind velocities v_w (speed and direction) measured at the elevation of the plate (1.05 m above ground level) with the aid of a cup anemometer ranged from 0 m/s to 3.6 m/s. Only data obtained during fairly steady winds in a particular direction perpendicular to one edge of the test plate were retained for evaluation purposes. The ambient air temperature was measured at the anemometer. Only test data obtained during clear sky conditions were used in the evaluation of h .

Two sets of experiments were conducted. In one case the upper surface of the plate was painted with a matt black paint having an absorption coefficient of $\alpha_p = 0.9$ and an emissivity of $\epsilon_p = 0.9$. A second set of tests was conducted with the plate covered by an aluminium foil with $\alpha_p = 0.1$ and $\epsilon_p = 0.03$.

The α_p and ϵ_p for both the aluminium surface and the black surface were determined experimentally and are in good agreement with values quoted in available literature.

Results

At wind speeds of $v_w = 0$, heat transfer from the plate to the ambient air is due to natural convection.

The heat transfer coefficient determined according to eqn. (5) for the measured data sets can be correlated by the following dimensionless equation

$$\begin{aligned} \frac{h_{nc} L}{k} &= \text{Nu}_{nc} \\ &= 0.227 \left[\left\{ \frac{2(T_p - T_a) g L^3 \rho^2}{(T_p + T_a) \mu^2} \right\} \left\{ \frac{\mu c_p}{k} \right\} \right]^{1/3} \\ &= 0.227 (\text{Gr Pr})^{1/3} \end{aligned} \quad (6)$$

Measured experimental data were compared to eqn. (6) and to a correlation proposed by Lloyd and Moran³

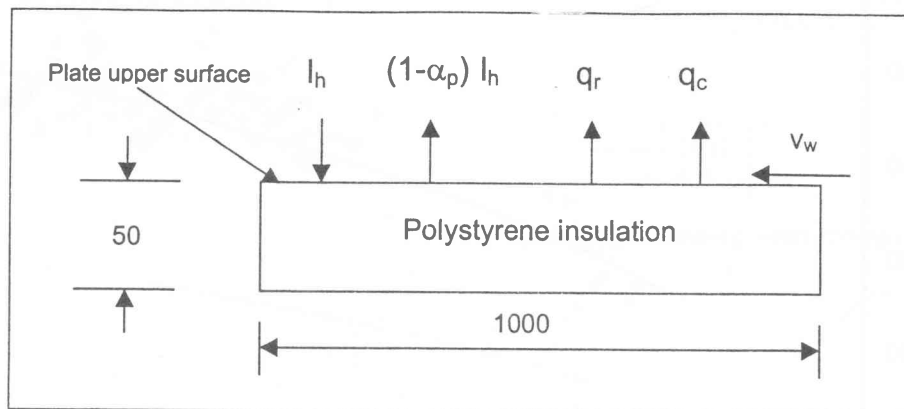


Figure 1 Insulated flat plate exposed to environment

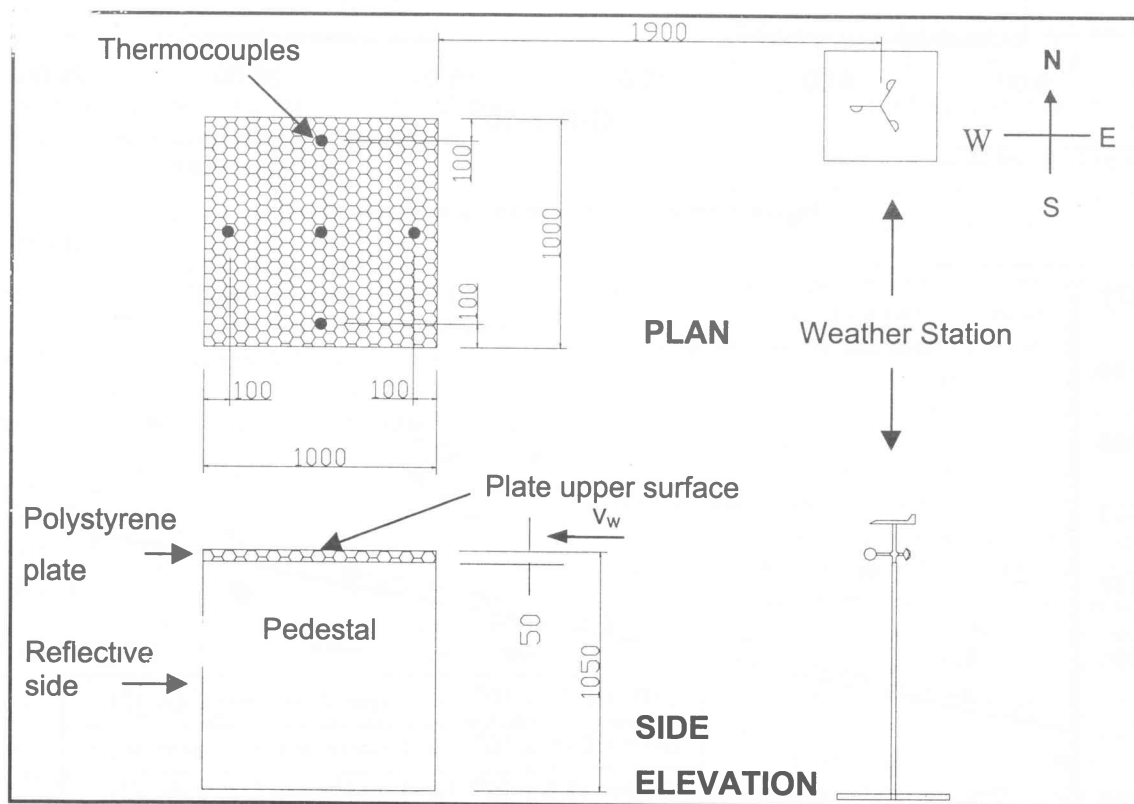


Figure 2 Experimental apparatus

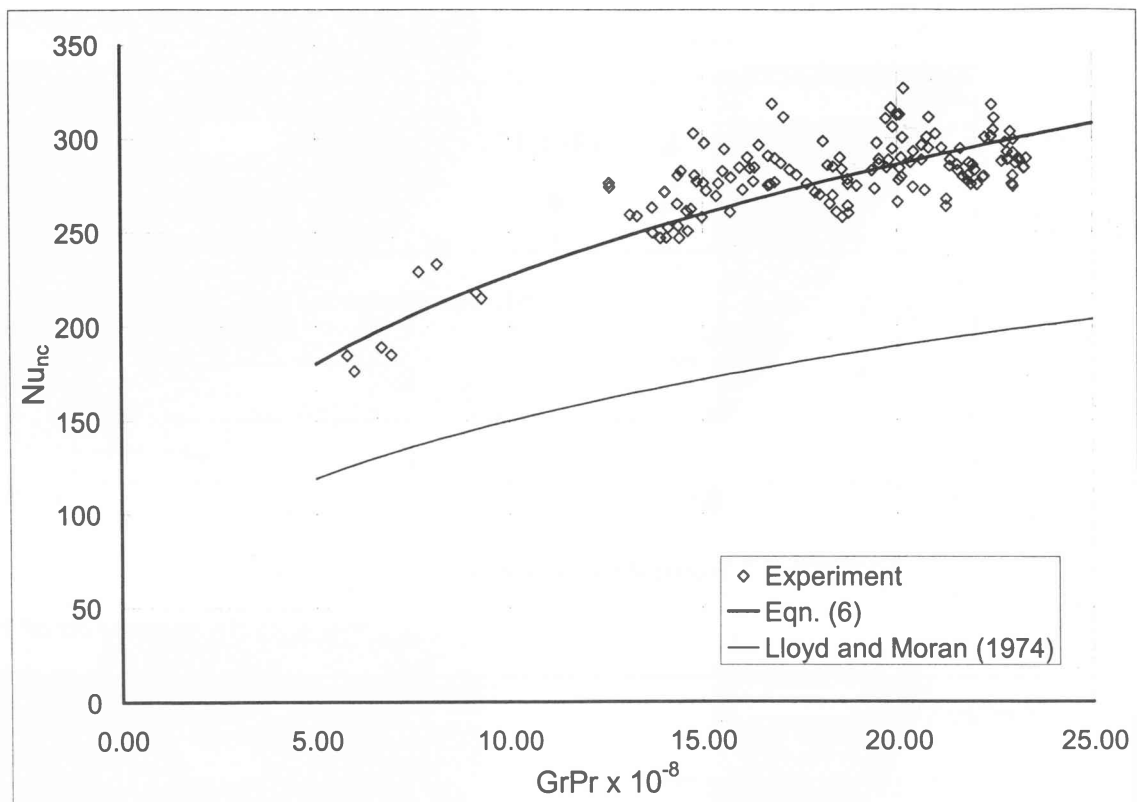


Figure 3 Heat transfer due to natural convection

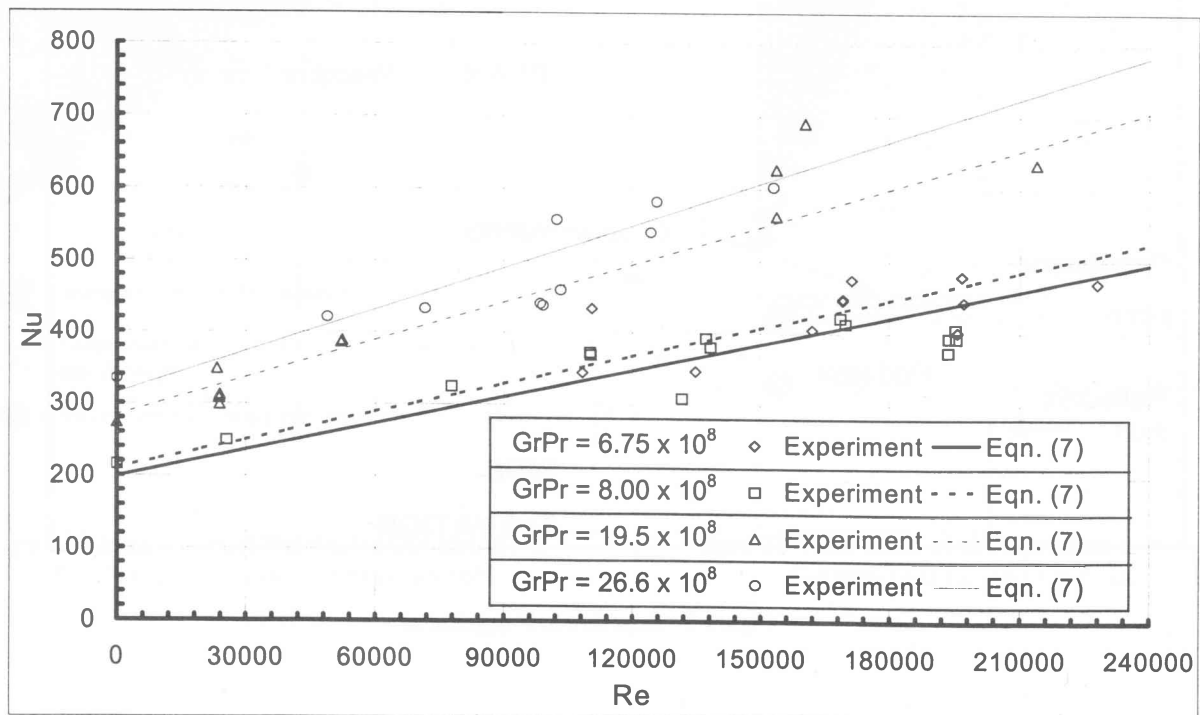


Figure 4 Convective heat transfer between horizontal plate and environment

for a heated horizontal surface facing upwards as shown in Figure 3. Note that the effective length dimension for both correlations in Figure 3 is the plate side length L .

According to Rohsenow *et al.*,⁴ natural convection will usually dominate when $Gr \geq 1100 Re^{3/2}$ while forced convection (windy conditions) will be the primary mechanism when $Gr \leq 11 Re^{3/2}$.

During windy conditions the airflow pattern across the test surface becomes very complex and the heat transfer coefficient becomes a function of both the Grashof (Gr) and Reynolds (Re) numbers.

As shown in Figure 4, the present data are well correlated by the following equation:

$$Nu = (Gr Pr)^{1/3} (0.227 + 1.406 \times 10^{-6} Re) \quad (7)$$

This equation is valid in the range $6.75 \times 10^8 \leq (Gr Pr) \leq 26.6 \times 10^8$ and for $0 \leq Re \leq 2.5 \times 10^5$.

Eqn. (7) correlates the data with a root-mean-square (RMS) value of 16.2 %. The RMS is defined as follows

$$RMS = \sum_{i=1}^n (Nu_{ex} - Nu_{cor})^2 / n \quad (8)$$

Numerical examples for evaluation of the Nusselt numbers are presented in Appendices A and B.

Conclusion

An equation that predicts the effective convective heat transfer on a horizontal heated plate exposed to the environment is presented. It should be noted that eqn. (7) is only applicable to a particular geometry. The range of operating conditions is clearly specified.

The fact that the present correlation (eqn. (6)) for heat transfer due to natural convection is higher than the prediction according to Lloyd and Moran³ may in part be due to the nature of the turbulence in the unstable ambient air and the geometry of the particular apparatus.

During windy conditions the nature of the flow of the air across the test surface will determine the heat transfer coefficient. For laminar flow over a surface $Nu_l \propto Re^{0.8}$ while for turbulent flow $Nu_t \propto Re^{0.8}$. In the present investigation eqn. (7) shows $Nu \propto Re$. Due to relatively high free stream turbulence a Reynolds number exponent of 0.8 is not unrealistic since it is likely that turbulent flow will predominate although the test surface is not very long in the flow direction. Further flow distortions due to separation along the edge of the test surface and due to natural convection can be the reason for the Reynolds number exponent of unity over the range tested.

Although it may be argued that the sky temperature according to Swinbank⁶ is not the most accurate of equations, this would imply that the effective convective heat transfer coefficient, as defined by eqn. (5), is similarly not very accurate. In the evaluation of the heat transfer rate from the plate to the natural environment this possible inaccuracy will be of little significance if the convection and

radiation effects are used in combination, i.e.

$$\begin{aligned} q &= (q_c + q_r) \\ &= k (Gr Pr)^{1/3} \\ &\times (0.227 + 1.406 \times 10^{-6} Re) (T_p - T_a) / L \\ &+ \sigma \epsilon_p (T_p^4 - T_{sky}^4) \end{aligned} \quad (9)$$

where $T_{sky} = 0.0552 T_a^{1.5}$.

References

1. Duffie JA & Beckman WA 1991. *Solar Engineering of Thermal Processes*, 2nd edn, pp.174–176. Wiley Interscience, New York.
2. Kumar Subodh, Sharma VB, Kandpal TC & Mullick SC 1997. Wind induced heat losses from outer cover of solar collectors. *Renewable Energy*, **10**, pp.613–616.
3. Lloyd JR & Moran WP 1974. Natural convection adjacent to horizontal surface of various platforms. *Trans. ASME J. of Heat Transfer*, **96**, p.417.
4. Rohsenow Warren M, Hartnett James P & Cho Young I 1998. *Handbook of Heat Transfer*, 3rd edn, pp.4.8–4.17. McGraw-Hill, New York.
5. Sharples S & Charlesworth PS 1998. Full-scale measurements of wind-induced convective heat transfer from a roof-mounted flat-plate solar collector. *Solar Energy*, **62**, pp.69–77.
6. Swinbank WC 1963. Long-wave radiation from clear skies. *Quart. J. Royal Meteorology Soc.*, **89**, pp.339–348.
7. Watmuff JH, Charters WWS & Proctor D 1977. Solar and wind induced external coefficients for solar collectors. *COMPLES*, **56**, No.2.

Appendix A: Numerical example

Natural Convection

On 13 May 2000, at 10:00, the following temperatures, pressure and incident solar radiation were measured:

$$\begin{aligned} T_a &= 23.7^\circ\text{C} &= 296.85\text{ K} \\ T_p &= 44.726^\circ\text{C} &= 317.876\text{ K} \\ I_h &= 391.152\text{ W/m}^2 \\ p_a &= 100989\text{ N/m}^2 \end{aligned}$$

The thermophysical properties of the air as well as the Prandtl and Grashof numbers are evaluated at a mean air-plate temperature.

$$\begin{aligned}
T_{ap} &= (296.85 + 317.876) / 2 = 307.363 \text{ K} \\
\rho &= 1.1447 \text{ kg/m}^3 \\
c_p &= 1007.242 \text{ J/kg K} \\
k &= 0.02679 \text{ W/m K} \\
\mu &= 1.8806 \times 10^{-5} \text{ kg/m s}
\end{aligned}$$

$$Pr = \frac{\mu c_p}{k} = \frac{1.8806 \times 10^{-5} \times 1007.242}{0.02679} = 0.707$$

$$\begin{aligned}
Gr &= \frac{2(T_p - T_a)gL^3\rho^2}{(T_p + T_a)\mu^2} \\
&= \frac{2 \times (317.876 - 296.85) \times 9.81 \times 1.0^3 \times 1.1447^2}{(317.876 + 296.85) \times (1.8806 \times 10^{-5})^2} \\
&= 2.4864 \times 10^9
\end{aligned}$$

According to eqn. (5), the experimental heat transfer coefficient is

$$\begin{aligned}
h_{nc} &= \frac{\alpha_p I_h - \sigma \epsilon_p \left\{ T_p^4 - (0.0552 T_a^{1.5})^4 \right\}}{T_p - T_a} \\
&= \left(\frac{0.9 \times 391.152 - 5.67 \times 10^{-8}}{\times 0.9 \left\{ 317.876^4 - (0.0552 \times 296.85^{1.5})^4 \right\}} \right) \\
&/ (317.876 - 296.85) \\
&7.382 \text{ W/m}^2 \text{ K}
\end{aligned}$$

The corresponding Nusselt number is

$$Nu_{nc} = \frac{h_{nc}L}{k} = \frac{7.382 \times 1.0}{0.02679} = 275.55$$

Appendix B: Numerical example

Forced convection

At 13:40 on 13 May 2000 the following pressure, temperatures, wind speed, and incident solar radiation were measured:

$$\begin{aligned}
T_a &= 29.9^\circ\text{C} &= 303.05 \text{ K} \\
T_p &= 56.356^\circ\text{C} &= 329.506 \text{ K} \\
I_h &= 574.07 \text{ W/m}^2 \text{ K} \\
p_a &= 100989 \text{ N/m}^2 \\
v_w &= 0.9 \text{ m/s}
\end{aligned}$$

Making use of these experimental values, the thermo-physical properties and the Prandtl, Grashof and Reynolds numbers of the air are evaluated at a mean air-plate temperature.

$$\begin{aligned}
T_{ap} &= (303.05 + 329.506) / 2 = 316.287 \text{ K} \\
\rho &= 1.1125 \text{ kg/m}^3 \\
c_p &= 1007.658 \text{ J/kg K} \\
k &= 0.02747 \text{ W/m K} \\
\mu &= 1.9211 \times 10^{-5} \text{ kg/m s}
\end{aligned}$$

$$Pr = \frac{\mu c_p}{k} = \frac{1.9211 \times 10^{-5} \times 1007.658}{0.02747} = 0.7047$$

$$\begin{aligned}
Gr &= \frac{2(T_p - T_a)gL^3\rho^2}{(T_p + T_a)\mu^2} \\
&= \frac{2 \times (329.506 - 303.05) \times 9.8 \times 1.0^3 \times 1.1125^2}{(329.506 + 303.05) \times (1.9211 \times 10^{-5})^2} \\
&= 2.7518 \times 10^9
\end{aligned}$$

$$Re = \frac{\rho v_w L}{\mu} = \frac{1.1125 \times 0.9 \times 1.0}{1.9211 \times 10^{-5}} = 52118.58$$

According to eqn. (5) the heat transfer coefficient is equal to

$$\begin{aligned}
h &= \frac{\alpha_p I_h - \sigma \epsilon_p \left\{ T_p^4 - (0.0552 T_a^{1.5})^4 \right\}}{T_p - T_a} \\
&= \left(\frac{0.9 \times 574.07 - 5.67 \times 10^{-8}}{\times 0.9 \left\{ 329.506^4 - (0.0552 \times 303.05^{1.5})^4 \right\}} \right) \\
&/ (329.506 - 303.05) \\
&10.663 \text{ W/m}^2 \text{ K}
\end{aligned}$$

which leads to a corresponding Nusselt number of

$$Nu = \frac{hL}{k} = \frac{10.663 \times 1.0}{0.02747} = 388.17.$$