Rain Attenuation Prediction Using Artificial Neural Network for Dynamic Rain Fade Mitigation

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Abstract— Atmospheric processes from which rainfall is formed are complex and cannot be accurately predicted using mathematical or statistical models. In this paper, the backpropagation neural network (BPNN) is trained to predict rainfall rates, and hence attenuation that is likely to be experienced on a link. This study is carried out over the subtropical region of Durban, South Africa (29.8587°S, 31.0218°E). Utilizing the non-linear mapping capability between inputs and outputs, the backpropagation neural network is trained using rainfall data collected from 2013 to 2016 to predict rainfall rates. Long-term rain attenuation statistics arising from predicted rain rates are compared with actual and ITU-R model, and results show a relatively small margin of error between predicted rain attenuation exceeded for 0.01% of an average year. Furthermore, analysis of predicted and actual rain attenuation within individual rain events from different rainfall regimes was carried out and results show that the proposed model can be used to predict the state of the link. This is demonstrated when the trained BPNN was tested using unseen data that was collected from January 2017 to May 2018, a period that spans through all four different climatic seasons of summer, autumn, winter and spring. Results of the test show a correlation coefficient of 0.8298. Finally, the proposed rain prediction model was tested on rainfall data from Butare, Rwanda (2.6078°S, 29.7368°E), which is a tropical region and results obtained indicate the portability of the proposed model to other regions.

Index Terms—artificial neural network, backpropagation neural network, rain attenuation, rain rate

I. INTRODUCTION

Satellite and terrestrial microwave links operating at frequencies above 10 GHz may suffer from signal outages during a heavy rainfall event [1-4]. Continuous streaming of content may thus be compromised during point-to-point (PP) communication. Live streaming of content like prime news and sport events demand virtually zero link outages. Rainfall is a natural phenomenon that attenuates the signal along the wireless communication link and, therefore, it becomes mandatory to mitigate rain attenuation for continuous content streaming. On this premise, dynamic fade mitigation techniques can be employed in conjunction with fade prediction models which are capable of predicting the state of the link. Accordingly, measures can be taken to ensure that the link is fully available for communication even in the advent of a rainfall storm event. Many researchers, including [5-8], have used an artificial neural network (ANN) for rainfall forecasting, and showed that the ANN can give acceptable results after training. In this paper, a backpropagation neural network (BPNN) is used to predict and classify rain attenuation for dynamic rain attenuation mitigation.

This paper is a detailed extension of work originally reported in [8]. In the current paper, additional material include: (1) retraining the BPNN with complete 2016 data, contrary to [8] where some data was set aside for testing and validation of the training network; (2) generation of CCDFs for predicted rain rates and rain attenuation, and (3) classification of predicted rain attenuation. The paper is structured as follows: Section 2 gives a summary of related work whereas Section 3 describes the artificial neural network as a computing unit. In Section 4, the methodology of this work is given while in Section 5 the analysis of results is carried out. The proposed prediction model is validated in Section 6 and the work is concluded in Section 7.

II. RELATED WORK

Studies on the application of artificial neural networks in the prediction of rainfall and rainfall rates have been on the rise, with most applications geared towards the field of water management and meteorology [6, 9-12]. French et al. [13] used an artificial neural network in forecasting a 2-dimensional rainfall one hour in advance. Their work became a good ground for most researchers to lay and advance studies in this area.

In 1995, Michaelides et al., [9] used an ANN in conjunction with daily rainfall observations in the neighboring sites to estimate missing rainfall data over Cyprus. Christodoulou et al., [5] trained the self-organizing map (SOM) and K-Nearest Neighbor (KNN) machine learning classifiers using radar data as inputs and rain gauge data as outputs to predict rainfall rate in Italy.

III. THE ARTIFICIAL NEURAL NETWORK COMPUTING TOOL

The neural network as a computing unit is divided into two functional parts: an integration function part, which sums the \( N \) inputs into a single value; and the output (or activation) function, which produces an output in accordance with the function of computation. The common activation function is the sigmoid function which possesses two beneficial properties namely: (1) continuity and, (2) differentiability of the error function during training. A simplified diagram of this computing unit and the training structure are shown in Fig. 1 and Fig. 2, respectively.
Integration and activation functions shown in Fig. 1 are given by [8, 14]:

\[ g = b + \sum_{n=1}^{N} w_n i_n \quad n = 1, 2, ..., N \]  
\[ f(g) = \frac{1}{1 + e^{-g}} \]  

where \( g \) is the integration function, \( b \) is the bias input, \( f \) is the activation function, \( N \) is the number of inputs, \( w_n \) is the \( n \)th weight and \( i_n \) is the \( n \)th input.

The actual output of the BPNN is obtained by the application of the activation function to the summation function as shown in (2). Thereafter, evaluation of the network’s performance is done during training by computing an error, \( E \), given by [14, 15]:

\[ E = \frac{1}{N} \sum_{n=1}^{N} (O_n - O_a)^2 \]  

where \( O_a \) is the actual output, \( O_t \) is the desired output (target) and \( H \) is the number of data points. Errors in (3) are minimized using an error derivative given by [8, 14]:

\[ \frac{\partial E_{total}}{\partial O_i} = -(O_t - O_a) \]  

An optimized weight vector, \( w \), that provides a minimized error function is achieved by updating associated weights using the expression,

\[ \Delta w_i = \eta \frac{\partial E}{\partial w_i} \quad i = 1, 2, ..., I \]  

where \( \eta \) is the learning rate, \( i \) is the input, \( \Delta w_i \) is the weight change on the \( i \)th input and \( O_t \) and \( O_a \) are the output contributed by the \( i \)th input.

The main objective in (3) is to find a minimized error function with \( \nabla E = 0 \) for prediction of a future rainfall rate \( R_d(t + 1) \) mm/h, given by [8]:

\[ R_p(t + 1) = f(R_a(t - 2), R_d(t - 1), R_d(t)) \]  

where \( R_d(t) \) is the actual rainfall rate at time \( t \), \( R_d(t - 1) \) is the actual rain rate at time \( t - 1 \) and \( R_d(t - 2) \) is the actual rain rate at time \( t - 2 \). All rain rates being in mm/h.

Most rain rate prediction models predict rain rates exceeded at various percentages of time in an average year. Some of these models include the work of [16] and [17]. For rain attenuation prediction, various prediction models have been proposed and include Bryant model [18], SC EXCELL model [19], Crane two-component model [20], SST model [21] and ITU-R model [22].

In this study, the SST model proposed by Matricciani [21] and the ITU-R model [22] are used for prediction of attenuation due to rain. For the model proposed in [21], the vertical structure of rain is modelled as two layers of precipitation, layer A (hydrometeors in the form of rain drops) and layer B (melting hydrometeors). In addition, the ITU-R P.618-13 also provides a model for prediction of rain attenuation exceeded for different percentages of time in an average year. This model is given in [22]:

\[ A_p = A_{0.01} \left( \frac{P}{0.01} \right)^{-0.655 + 0.033 \ln(p) - 0.045 \ln(a_{0.01}) - \beta (1 - p) \sin \theta} \]  

and:

\[ A_{0.01} = k R_{0.01} e^{L_{eff}} \quad [dB] \]  

where \( p \) is the probability of exceedance in %, \( A_p \) is the attenuation exceeded \( p \) % of time in an average year, \( A_{0.01} \) is the attenuation exceeded 0.01 % of time in an average year, \( \beta \) is the parameter dependent on the latitude of the earth station, and \( \theta \) is the angle of elevation of the earth station antenna, and \( L_{eff} \) is the effective slant path length, with both \( \beta \) and \( \theta \) as obtained in [22], \( k \) and \( \alpha \) are parameters dependent on frequency.

Rain attenuation time series obtained from the SST model proposed by [21] is given by:

\[ A(t) = k_d R(t) a_A L_A + r a_k R(t) a_B (L_B - L_A) \]  

where \( A(t) \) is rain attenuation, in dB, at time \( t \), \( L_A \) and \( L_B \) are precipitation layer and the melting layer slant paths, respectively, in km, \( R(t) \) is the rain rate in layer A, \( r \) is rain rate in layer B whose value is given in [21], whereas \( k_d, a_A, k_B \), and \( a_B \) are frequency-dependent parameters for layer A and layer B given in [23].

IV. METHODOLOGY

Data for training and validating the BPNN model proposed in this work was collected at the University of KwaZulu-Natal, Durban, through a JWD, RD-80 impact type disdrometer with a sampling time of 30 seconds. Additional details and setup are given in [4, 8]. Training data was collected for a period of four years from 2013 to 2016. This dataset comprises of four rainfall regimes from drizzle to super storms and the total number of training samples used was 108,861. Validation and testing data was drawn from data collected from January 2017 to May 2018.
Rainfall data within this period of 17 months are a representation of all four seasons (summer, autumn, winter and spring) that are experienced in South Africa.

V. RESULTS AND ANALYSIS

This section presents the analysis of results that were obtained from the study.

A. BPNN Training

A three-layered network with three neurons in the input layer (I), three neurons in the hidden layer (H) and one neuron in the output layer (O) was used during training as shown in Fig. 2. This architectural structure is simplified as 3:3:1:1, where the last ‘1’ represents the network output and not a neuron.

The artificial neural network was trained using TRAINLM training function and LEARNGDM as the adaptation learning function. Performance functions chosen were the mean squared error (MSE) and TANSIG transfer function. Training, testing and validation results are shown in Fig. 3 and Fig. 4.

During the neural network training, the best performance reached was the optimum mapping of outputs and targets at epoch 371 of 377 epochs with a mean square error of 6.017. The training performance plot is shown in Fig. 3. Similarly, Fig. 4 shows the training regression plot with a regression coefficient, $R^2 = 0.91094$ which shows a good correlation between the actual outputs and predicted outputs.

Optimized weight and bias matrices that were obtained during the training process are shown in (10).

\[
\begin{align*}
    w_{HI} &= \begin{bmatrix} -0.1974 & -1.1467 & -7.8568 \\ -0.0115 & 0.0086 & -0.0476 \\ 4.0797 & 6.1838 & 6.0543 \end{bmatrix} \quad (10a) \\
    w_{OH} &= \begin{bmatrix} -78.4395 & -32.0736 & 31.939 \end{bmatrix} \quad (10b) \\
    b_H &= \begin{bmatrix} -11.4485 \\ 0.4845 \\ -17.3805 \end{bmatrix} \quad (10c) \\
    b_O &= \begin{bmatrix} -32.1027 \end{bmatrix} \quad (10d)
\end{align*}
\]

where $w_{HI}$ is the weight vector for weights from the input to the hidden layer, $w_{OH}$ is the weight vector for weights from the hidden layer to the output layer, $b_H$ is the input bias vector to the hidden layer, and $b_O$ is the bias input to the output layer.

In Fig. 5, the unseen model testing dataset was sourced from 2017-2018 rainfall data. This data is ‘unseen’ to the trained network because it was not used during training. Results of testing show a fair correlation of $R^2 = 0.8298$. Further, this complete model testing dataset was compared to the output of the trained neural network and an overall root mean square error (RMSE) value of 2.5128 was realized. Fig. 6 shows the correlation between the ANN predicted output and the current or actual output. The correlation between these two outputs is 0.9811. This correlation implies that the current output can be used to predict a future rain rate at time $(t + 1)$. This prediction can be deduced from the relationship shown in Fig. 6 and is given by:

\[
    R_p(t + 1) = mR_a(t) + n \quad (11)
\]

where $m$ and $n$ are regression parameters whose values are 0.9036 and $n = 0.3483$, respectively. Consequently, from (9) and (11), link attenuation at time $(t + 1)$ can be predicted by:

\[
    A_p(t + 1) = \Phi L_A + \Psi (L_B - L_A) \quad (12a)
\]

with:

\[
    \Phi = k_A R_p(t + 1)^{\alpha_A} \quad (12b) \\
    \Psi = r^{\alpha_B} k_B R_p(t + 1)^{\alpha_B} \quad (12b)
\]

B. Complementary cumulative distribution functions

CCDFs aid in the determination of acceptable link fade margins by providing information on different percentages of parameter exceedances for an average year. For system design engineers, the parameter of ultimate importance is the rain rate exceeded for 0.01 % ($R_{0.01}$) and 0.001 % ($R_{0.001}$) of time in an average year [4, 24, 25]. In this paper, rain rate and rain attenuation CCDFs are derived from rainfall data collected
from January 2017 to May 2018. Fig. 7 and Table I shows long-term rain rate statistics for actual rain rates, ANN predicted rain rates and modelled rain rates. In Fig. 7, it is seen that rain rates exceeded for various percentages of time in an average year are close for the three distributions for percentages below 0.01. For the ANN output, the values are close to actual values for almost all percentages.

From Fig. 7, it is seen that the rainfall rate exceeded for 0.01 % of time in an average year is 177 mm/h and 178 mm/h for actual and predicted outputs, respectively. For the model, this value is 160 mm/h. Similarly, Fig. 8 and Table II show resultant long-term rain attenuation statistics for both actual and predicted rainfall rates.

The ITU-R rain attenuation model is also included for comparison of exceedances at various percentages. It is revealed that attenuation exceeded for 0.01 % of an average year is 53 dB (actual rain rates), 50 dB (ANN predicted rain rates), 48 dB (proposed model) and 53 dB (ITU-R model).
VI. RAIN ATTENUATION PREDICTION AND PREDICTION MODEL VALIDATION

The applicability of the trained neural network and the proposed model was tested on different rainfall events from different rainfall regimes. Five attenuation classes with attenuation thresholds at 10 dB, 20 dB, 40 dB and 60 dB were used to show the suitability of the proposed model in the prediction of rainfall attenuation for dynamic rain fade mitigation. These attenuation classes are shown in Table III.

Tests on the trained prediction model were carried out on individual rain events across different rain regimes. For instance, Fig. 9(a) shows the comparison of predicted and actual rain rate time series. In this figure, rain rate times series within a rain event with a maximum rain rate of 22.2265 mm/h was tested against ANN predicted outputs and model outputs.

Using attenuation classifications shown in Table III and Fig. 9(b), we show that the predicted rain attenuation values are within the expected bound of $\lambda < 10$ dB (Level 1). A good agreement is observed when the ‘o’ and ‘x’ markers merge on the graph as seen in Fig. 9(b).

Similarly, Fig. 10(a) and Fig. 10(b) show rain rates and attenuation comparison between the model output and actual outputs. Once more, the model attenuation class outputs are within expected classes.

In Fig. 11(a), the model output is tested on a rain event with a maximum rain rate of 89.9575 mm/h. From this rain event, there are three attenuation levels, 1-3, with a few misses in the predicted rain attenuation as seen in Fig. 11(b).

![Fig. 9](image1.png)  
(a) Rain rate prediction (BPNN out) (b) classification of predicted attenuation levels for storm event of 15th May, 2017, 23:03:30 hours  

![Fig. 10](image2.png)  
(a) Rain rate prediction (model) (b) classification of predicted attenuation levels for Storm event of 15th May, 2017, 23:03:30 hours  

![Table III](table.png)  

TABLE III  
RAIN ATTENUATION CLASSES

<table>
<thead>
<tr>
<th>Attenuation Class</th>
<th>Class Bounds [dB]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\lambda &lt; 10$</td>
</tr>
<tr>
<td>2</td>
<td>$10 \leq \lambda &lt; 20$</td>
</tr>
<tr>
<td>3</td>
<td>$20 \leq \lambda &lt; 40$</td>
</tr>
<tr>
<td>4</td>
<td>$40 \leq \lambda &lt; 60$</td>
</tr>
<tr>
<td>5</td>
<td>$\lambda \geq 60$</td>
</tr>
</tbody>
</table>
Within the testing dataset, the highest rain rate observed was 224.9989 mm/h within a rain event of 22nd February, 2017 at 10:53:00 hours, over Durban. This event is shown in Fig. 13(a). In this figure, it is seen that five attenuation levels are obtained up to the highest attenuation class of level 5. A view of a detailed section of Fig. 13(b) is shown in Fig. 14, in which there are nine misses during the period of deep fading within 600 s from time $t = 1000$ s to $t = 1600$ s. However, cases where the ‘x’ marker is above the ‘o’ maker can be considered safer because during these instances, attenuation is overestimated, which means that a fade mitigation measure will be effected. Additionally, further analysis shows that overestimation or underestimation of these rain attenuation, in most cases, involves two adjacent levels. Additional analysis shows that instances of sharp spikes are rare and short-lived. More importantly, these results show that the ANN model is able to predict deep fades on the link (Level 5) as seen in Fig. 14.
To ascertain the portability of the proposed model, rainfall data sampled at 1-minute integration time was used to test the model with a rain event from Butare, Rwanda, a region with equatorial climate. Results of this test are shown in Fig. 15. Analysis of this test is presented in Fig. 15(b) and shows that there are three misses within a period of 600 s, which, excluding overestimation, reduces to only one miss for a case of underestimation at time $t = 9750$ s.

VII. CONCLUSION

This study has established that a backpropagation neural network can satisfactorily be used to predict the state of the link during a rainfall event for dynamic rain fade mitigation. Results show that the trained backpropagation neural network is able to predict deep fades sufficiently well during a super storm rain event. Additionally, the proposed model can be portable to other locations with different geographical climates, provided that the sampling time is relatively low, that is, from one-minute and below. The proposed model, however, may give inaccurate results when used with data sampled at relatively long intervals. For better results, the sampling time should be one-minute and less as recommended by ITU Radiocommunication. Further, the proposed model can be improved by training the BPNN with rain rates of relatively lower sampling time, as low as 10 s. This allows detection of shorter rain spikes for a more accurate link state prediction.

REFERENCES

Her research interests focus on microwave and millimeter wave propagation studies with special interests in the effects of rain on the performance of earth-satellite communication links and dynamic rain fade mitigation techniques.

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